Preparation and structural studies in the $(70 - x)TeO₂ - 20WO₃$ $10Li₂O-xLn₂O₃$ glasses

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Abstract Quaternary tellurite glass systems $(70 - x)$ TeO₂–20WO₃–10Li₂O–xLn₂O₃ where $x = 0, 1, 3$ and 5 mol% and Ln are La, Pr, Nd, Sm, Er and Yb, respectively, have been prepared by the melt quenching technique. Densities of the obtained glasses were measured and the molar volume was calculated. IR absorption spectra of the present glass systems were determined at room temperature over the range of wavenumbers from 400– $1,600 \text{ cm}^{-1}$. Raman spectra of the present glass samples were measured in the range of $30-1,030$ cm⁻¹. Density, molar volume, IR and Raman spectra of the glasses were discussed by calculating average cross-link density, packing density, theoretically calculated Poisson's ratio and number of bonds per unit volume of the studied glasses. Also, the quantitative interpretations were based on concentration of ions per unit volume of Te , Ln and O , short distance in nanometre between ions for $(Te-O)$ of $TeO₄$ and TeO₃ groups, (W–O) of WO₄, WO₆ groups and calculated wavenumber, \bar{v} , for TeO₄ and TeO₃, respectively. The average stretching force constant that present in these quaternary glasses has been calculated in order to interpret the data obtained.

Introduction

Structural studies in glasses are of great important owing to the interrelation between the atomic arrangement and properties. While this interest is primarily on the technological side, structural on glasses offer a unique possibility

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to evaluate theories and structural models developed over the last decades [\[1](#page-8-0)]. To comprehend structural details, a common strategy is to change the glass structure either by adding network modifiers or by interrogating the material with some external stimuli such as heat or pressure. Tellurium oxide is an interesting case where the basic building block of structure experiences considerable changes either by modifiers or by increasing temperature, though being of three-dimensional geometry. Tellurite-oxide based glasses have been considered as promising materials for use in non-linear optical devices or host materials for upconversion fluorescence of rare earth ions [\[2–10](#page-8-0)]. They are characterized by high refractive index values (larger than 2.0 in most cases) $[11]$ $[11]$, wide infrared transmittance $[12]$ $[12]$, high thermal expansion and good chemical durability. So, it is of interesting to investigate the structure of the tellurite glass especially when the glass doped with different rare earth ions. Crystalline $TeO₂$ has a unique structural unit that is, an asymmetrical $TeO₄$ trigonal bipyramid (tbp), in which there are two different kinds of sites, two axial and three equatorial positions. One of the latter is occupied by a lone pair of electrons. The structural of $TeO₂$ based glasses is of interest, because there are two types of basis structural unit, i.e. $TeO₄$ tbp with a lone pair electron in an equatorial position and $TeO₃$ trigonal pyramid (tp). The tellurite glass system is an important amorphous system considered to have important commercial applications in optical communication due to its high refractive index, good infrared transmittance and high optical non-linearity. Tellurite glass is a good host material for laser applications. Tellurite glasses doped with rare earth ions are also candidates for excitations, absorption, photoluminescence at different colors as mentioned previously [\[8](#page-8-0), [9\]](#page-8-0).

In the present work, the structure of the prepared glass system $(70 - x)$ TeO₂-20WO₃-10Li₂O-xLn₂O₃ where $x = 0$, 1, 3 and 5 mol.% Ln: La, Nd, Sm, Er, Yb and $Pr₆O₁₁$ were investigated by using infrared and Raman spectroscopy in addition of density and molar volume. Also the structure of the glasses is interpreted by calculated parameters like average cross-link density, Poisson's ratio, number of bonds per unit volume, bond length and stretching force constant. The effect of the concentration of the added rare earth ions on the structure, calculated and measured parameters is discussed.

Experimental technique

Glass preparation

The raw materials which used (TeO₂ from Alfa, LiCO₃ and $WO₃$ from Strem and rare earth oxides are from Prolabo) were of Analar Grade. The batches were melted at a maximum temperature of \sim 950 °C in a deep platinum crucible for 30–45 min in air. Then they could be poured into a heated brass mould to obtain cubic samples with dimensions about $1 \times 1 \times (0.6–1.0)$ cm³. The samples were annealed at \sim 250–300 °C for 1 h. The samples were also polished and prepared for the measurements.

The densities of the prepared samples were measured by the Archimedean method using $CCl₄$ as an immersion liquid. The molar volume was calculated by the equation $V_{\rm m} = (M/\rho)$, where ρ is the density and M the molecular weight of the glass sample, which is calculated as follows: $M = \sum_i (x_i)(w_i)$, where x_i and w_i are the mole fraction and molecular weight of the component i , respectively. The error of the density measurements was not more than ± 0.001 .

IR measurements

For infrared investigations, glass sample was ground in a clean mortar to fine powder. Fixed weight from glass powder and KBr (from Prolabo) were mixed and ground. Then transparent pellets were formed by pressing the mixture at 10 tons for a few minutes under vacuum. IR absorption spectra of the present glass systems were determined by using a Bomem Michelson 100 spectrophotometer. All measurements were carried out at room temperature over the range of wavenumbers from 400 to $1,600$ cm⁻¹.

Raman spectra measurements

Raman spectra of the present glass samples with two polished faces and approximately 6–10 mm in thickness were measured in the range of $30-1,030$ cm⁻¹ by using Olympus BHT microscope with $\times 50$ LF and $\times 100$ objectives

and the spectra are analyzed with a Dilor Z24 Raman spectrometer (single channel, triple monochromator) equipped with a photo-multiplier; an argon ion laser Coherent Innova 90-3. The Raman spectra were measured at university of Le Mans, France.

Results and discussion

Density and structure parameters

The compositions of the studied glasses are given in Table [1](#page-2-0). The values of the glass density and molar volume of the present tellurite glass doped with various rare earth oxides are given in Table [2](#page-2-0). The density values are comparable to those previously measured $(5.88-6.18 \text{ g/cm}^3)$ [\[13](#page-8-0)]. Figure [1](#page-3-0)a shows the variation of the glass density with the concentration of the rare earth oxides. It is seen that the density increase with increasing the rare earth oxides content. The density of Yb, Er and Pr doped glasses is higher than those of Sm, Nd and La doped glasses. The increase in the density is attributed to that the molecular weight of the added rare earth oxides (more than 300) is higher than that of $TeO₂$ (159.59). The molar volume increased with increasing the rare earth oxide contents as shown in Fig. [1](#page-3-0)b. The observed increase in the molar volume may be attributed to an increase in the bond length or the inter-atomic spacing between the atoms as given in Table [4](#page-6-0). The density of the glasses can be estimated from the density of their constituents according to this equation:

$$
\rho = \sum_{i} x_i \rho_i,\tag{1}
$$

where x_i is the mole fraction of the component i and ρ_i its density. The calculated and the measured values are in good agreements as collected in Table [2.](#page-2-0)

It is of interesting to calculate the average crosslink density of the present glasses, which is calculated according to this equation:

$$
\bar{n_c} = \frac{1}{\eta} [(n_c)_1 (N_c)_1 + (n_c)_2 (N_c)_2 + \cdots]
$$
\n(2)

where $n_c = n_f - 2$, n_f is the coordination number of the glass component, which equals 4 for $TeO₂$ and $Li₂O$, 6 for WO_3 , Er_2O_3 and Yb_2O_3 , 7 for Nd_2O_3 , Sm_2O_3 , La_2O_3 and $Pr₆O₁₁$, respectively.

$$
\eta = \sum_i (N_c)_i = \sum_i x_i n_i
$$

and n_i is the number of cations of the component *i*. The calculated values of \bar{n}_c are given in Table [2](#page-2-0).

The increase in the average crosslink density from 2.364 to 2.609 means that the addition of rare earth

Table 2 The density (measured and calculated), molar volume, average cross-link density, packing density, theoretically calculated Poisson's ratio and number of bonds per unit volume of the studied glasses

oxides to present TWL (TeO₂–WO₃–Li₂O) glass modify Te–O–Te by decreasing the tellurium atom coordination number from 4 to 3. This leads to creation of extra bridging oxygen atoms and increase the connectivity of the network $[14]$ $[14]$. This leads to increase the density as shown in Fig. [1a](#page-3-0).

The Poisson's ratio can be also calculated theoretically from the expression given by [[15\]](#page-8-0):

density with composition of $TeO₂–WO₃–Li₂O$ glass doped with rare earth oxides. b Variation of molar volume with composition of $TeO₂$ - $WO₃-Li₂O$ glass doped with rare earth oxides

calculated as follows:

$$
\mu_{\text{cal}} = 0.5 - \frac{1}{7.2 V_t} \tag{3}
$$

where

$$
V_t = \frac{\rho}{M} \sum_i x_i V_i \tag{4}
$$

and

$$
V_i = \frac{4\pi N}{3} (nR_A^3 + mR_O^3),\tag{5}
$$

where μ_{cal} is the theoretically calculated Poisson's ratio, V_t the packing density of the glass, ρ the glass density, M the glass molecular weight, x_i the mole fraction of the component i, V_i the packing factor of the oxide A_nO_m , N the Avogadro's number, R_A and R_O are the ionic radius of cation A and anion O , respectively.

The calculated packing factor for TeO_2 , WO_3 and Li_2O is equal to 41.05×10^{-6} , 21.42×10^{-6} , 8.01×10^{-6} m³ while equal to 25.22×10^{-6} , 26.43×10^{-6} , $27.11 \times$ 10^{-6} , 28.03 \times 10^{-6} , 28.42 \times 10^{-6} and 95.69 \times 10^{-6} m³ for Er₂O₃, Sm₂O₃, Nd₂O₃, Yb₂O₃, La₂O₃ and Pr₆O₁₁, respectively. So, by increasing the rare earth oxides with packing factor less than that of $TeO₂$, the packing density V_t of the glasses decreases and the calculated Poisson's ratio also decreased.

It is obtained that by increase the rare earth oxides instead of TeO₂ the Poisson's ratio, μ_{cal} , decrease from 0.385 of the blank sample (which undoped with rare earth (TWL)) to around 0.369 for the samples doped with rare earth oxides, Table [2](#page-2-0). It is known that Poisson's ratio is affected by the changes in the cross-link density of the glass network [\[16](#page-8-0)]. Which means that, the decrease in μ_{cal} is attributed to the increase in the cross-link density, which was observed in the present glasses by increasing of the

rare earth oxides instead of $TeO₂$, see Table [2.](#page-2-0) Also, a high cross-link density has Poisson's ratio in the order of 0.1 to 0.2, while a low cross-link density has Poisson's ratio between 0.3 and 0.5 [\[14](#page-8-0), [17,](#page-8-0) [18\]](#page-8-0). Also, the decrease of the calculated Poisson's ratio is attributed as mentioned before to the increase in the connectivity of the network linkages and the strong of the network structure of the glasses by adding the rare earth oxides. This can be interpreted by the

$$
n_{\rm b} = \sum n_s \frac{N \rho}{M},\tag{6}
$$

number of bonds per unit volume, n_b , of the glasses which

where n_s is the number of bonds per unit glass formula, $n_s = (coordination number of each cation) \times (number of$ cations in the glass formula unit), N the Avogadro's number, M the glass molecular weight and ρ its density.

The calculated values of n_b are given in Table [2](#page-2-0). As obtained from the above relation (6) and Table [2,](#page-2-0) the number of bonds per unit volume increases, e.g. for the present telluride glasses doped with $La₂O₃$ by 1 and 5 mol.% the number of bonds per unit volume increased from n_b 104.656–108.504 \times 10²¹ cm⁻³. Therefore, the glasses become more connective and rigid by doping the rare earth oxides into the studied glasses.

IR spectra

IR absorption spectra of the present glasses, undoped and doped with rare earth oxides such as Er_2O_3 , La_2O_3 , Pr_6O_{11} , Sm_2O_3 , Yb_2O_3 and Nd_2O_3 are shown in Fig. [2a](#page-4-0)–c, respectively. Their assigned band positions are reported in Table [3](#page-4-0). From these figures, it is shown that there are different absorption bands which, respectively, 500, 610,

Fig. 2 a Infrared absorption spectra of TeO₂–WO₃–Li₂O glasses doped with Er₂O₃ and La₂O₃. b Infrared absorption spectra of TeO₂–WO₃– Li₂O glasses doped with Pr₆O₁₁ and Sm₂O₃. c Infrared absorption spectra of TeO₂–WO₃–Li₂O glasses doped with Yb₂O₃ and Nd₂O₃

660, 780, 930, 1,055, 1,108 and 1,400 cm-¹ for the sample, which undoped with rare earth oxides. By adding $Ln₂O₃$ (rare earth oxides) to this sample instead of $TeO₂$, there are absorption band appeared at 440–470, 480–520, 650–680, 745–790, 930, 1,040–1,085, 1,092–1,107 and 1,492– 1,400 cm^{-1} , respectively as shown in Fig. 2a–c. The two bands that at 1,055 and 1,108 cm^{-1} of the undoped sample are combined to be one band at $1,085-1,045$ cm⁻¹ by

adding $Sm₂O₃$. From these Fig. 2a–c, its observed that, by adding the rare earth oxides to the present glasses instead of TeO₂ the band which at 600 cm⁻¹ of the undoped samples with rare earths was combined with the band which at 660 cm^{-1} and shifted to become around 650– 680 cm^{-1} as tabulated in Table 3.

According to the IR absorption spectra of the studied glasses, the absorption band which around 430–450,

440–460, 460, 450–460, 420–435 and 440–450 cm⁻¹ are assigned to be due to La–O, Pr–O, Nd–O, Sm–O, Er–O and Yb–O stretching vibrations, respectively. This means that a fraction of rare earth ions was incorporated in the network of these glasses and act as a network intermediate. The main broad intense absorption band which at around 660 cm^{-1} for the undoped glass sample and $650-680 \text{ cm}^{-1}$ of the glass sample doped with rare earths are assigned to be the bonding mode of Te–O–Te or O–Te–O linkages, the stretching mode $[TeO_4]$ tp with bridging oxygen. It is known that, the addition of different other components to tellurite glasses like WO_3 , Li_2O or Ln_2O_3 may cause the vibration of TeO₃ groups around 745–790 cm⁻¹ and that symmetric and antisymmetric stretching vibration of $TeO₃$ groups tp with NBO induces the peak around 745 cm^{-1} [\[19](#page-8-0)]. With an increase in rare earth oxides, e.g. La_2O_3 content to $TeO₂$ based glass, the coordination state of tellurium atom changes from TeO₄ tpb through TeO₃₊₁ polyhedra to $TeO₃$ tp, and NBO atoms increase in number. Glass having low $La₂O₃$ content have a continuous network structure composed mainly of TeO₄ tpb and TeO₃₊₁ polyhedra having one NBO atom, while glasses containing more than 15 mol% La_2O_3 contain small structural fragments composed of $TeO₃$ tps having two or three NBO atoms [\[20](#page-8-0)]. So that the number of NBO in the present glasses is very low, and this is the reason which it called that the glass is rigid and more connective. The peak at $420-460$ cm⁻¹, which appears by adding the rare earth oxides to the present glasses, may be due to Ln–O as described before, or Te–O–W bridging bonds, which would increase the network connectivity [[21\]](#page-8-0). The formation of Te–O–W bridging is expected because both W and Te atoms have comparable electronegativity and can therefore substitute for each other in bonding with O atoms [\[22](#page-8-0)]. That is a small fraction of W cations, which are incorporated in the glass network. The bands, which at 1,045, 1,092 and 1,100 cm^{-1} , are due to TeO₄ group. While the band at 930 cm⁻¹ is due to WO_4 tetrahedral and/or WO_6 octahedral group [[23\]](#page-8-0). It is obtained that most of the absorption band position in general are shifted towards the lower frequency region by doping the rare earth oxides to the present glasses. This is because the rare earth oxides are enter the glass network as intermediate and also it means that tellurite glass are good host material for rare earth ions. This result yields that the present glasses are good host for the rare earth ions for the optical properties studying the optical applications.

In order to calculate the wavenumber band position of the present glasses, we follow the following steps: the short distance between the ions can be calculated from the concentration of the ions A and O of the compound A_nO_m , which given as the following equations [[14,](#page-8-0) [24\]](#page-8-0):

$$
n(A) = \frac{n \times N}{100 V_{\rm m}},\tag{7}
$$

$$
n(O) = \frac{m \, x \, N}{100 \, V_{\text{m}}},\tag{8}
$$

where N , x and V_m are the Avogadro's number, mole fraction of A_nO_m and the glass molar volume respectively. Therefore, the short separation distances, r , between the identical A or O ions are given by:

$$
r = \sqrt[3]{\frac{1}{n}}\tag{9}
$$

According to Eqs. $7-9$, the calculated values of $n(Te)$, $n(O)$, $n(W)$, $r(Te-Te)$, $r(O-O)$ and $r(W-W)$ are given in Table [4](#page-6-0). Therefore, $r(Te-O)$ can be calculated for the $TeO₄$ group by considering the Te ions, which are lying in the centre of four oxygen ions, see Table [4](#page-6-0) for the obtained values. Also, $r(Te-O)$ for $TeO₃$ group can be calculated by considering the Te atom, which is put at the cross-point position of the vertical lines from the vertex of the equal ribs triangle with its vertices are the oxygen atoms, as shown in Table [4](#page-6-0) for obtained values. Therefore, the wavenumber position of the vibrated modes can be calculated as follows:

$$
\overline{v} = \frac{1}{2\pi c} \sqrt{\frac{F}{\mu}}
$$
 (10)

where

$$
F = \frac{1.7}{r^3} \tag{11}
$$

where c, F, μ and r are the velocity of light, stretching force constant, reduced mass between the cation–anion and r the calculated bond length between them in nanometre. All the calculated parameters are given in Tables [3](#page-4-0) and [4,](#page-6-0) respectively. The calculated wavenumber are reasonably compared with that the measured experimental from IR spectra. Figure [3](#page-7-0) shows the dependence of the stretching force constant, F , with the bond length of the Te groups. F decrease with increasing the bond length of main groups. For more structural details, Raman spectroscopy was used as shown in the next section.

Raman spectra

The Raman spectra of some of the present glasses undoped and doped with rare earths reveals also different absorption bands as shown in Fig. [4](#page-7-0)a, b, respectively. Two main absorption bands at around 700 and 930 cm^{-1} in addition of 480, 360, 220, 132 and 54 cm^{-1} , Table [5.](#page-7-0) By adding the rare earth oxides to the present glasses, these bands are affected and become at around 695–711, 930, 465–480,

339–348, 120–153 and 48–57 cm^{-1} in addition of new band around $735-745$ cm⁻¹, respectively, Table [5.](#page-7-0) It is seen that the band position, which at 930 cm^{-1} , does not changed by adding the rare earth oxides to the present glasses. The peak which at $695-711$ cm⁻¹ is assigned to be due to the vibration v_1 of TeO₄ group [\[25](#page-8-0)], while which at 930 cm⁻¹ band is due to v_1 of WO₄ tetrahedral group [\[23](#page-8-0)]. The absorption band which around $465-480$ cm⁻¹ is due to

Fig. 3 Variation of stretching force constant of a TeO₄ and b TeO₃ groups with the bond length of the studied glasses

TeO₄ group and 339–348 cm⁻¹ due to v_4 of TeO₄ group. The weak band at $150-120$ cm⁻¹ of the present glasses may relate to the $Li₂O$ vibrations [[26\]](#page-8-0). It should be noted that there is broad shoulder on this band, which is centred at 135 cm^{-1} . The very strong peak with a maximum, which at between $48-57$ cm⁻¹, is identified with the Boson Peak,

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Table 5 Raman absorption band position of some of TeO_2-WO_3 $Li₂O$ glasses doped with rare earth oxides

Sample no.	Boson peak	О		Li- TeO ₃ v_4 of TeO ₄ v_1 of TeO ₄		TeO ₄	TeO ₄ v_1 of	WO ₄
TWL	54		132 220	360	480	700		930
TWLNd1	48	153		342	470	705		930
TWLNd3	48	135		345	480	700	740	930
TWLEr1	48	150		342	480	702		930
TWLEr3	57	135		345	480	695	745	930
TWLSm1	48	135		348	480	711		930
TWLSm3 57			120 234	339	470	700	740	930
TWLYb1	48	126		342	460	705		930
TWLYb3	54	144		345	475	700	745	930
TWLLa1	51		135 220	342	460	708		930
TWLLa3 54		138		348	465	700	735	930

a feature characteristic of the vitreous state. Although various attempts have been made to explain the origin of the Boson Peak, it is generally accepted that it can be related to long-range spatial correlations in the structure [\[27](#page-8-0)]. The disorder resulting from the creation of the glass network yields a change in selection rules of the equivalent order state, thus allowing the activity of acoustic modes in the Raman spectrum [[28\]](#page-8-0). The peak intensity and the band position of the Boson peak are shown in Fig. [5.](#page-8-0) It is shown that they are in reverse behaviour. This leads to that the Boson peak is affected by the rare earth oxide additions. It is also seen that the TeO₄ band position $(695-711 \text{ cm}^{-1})$ shifts to higher wavenumber (lower frequency) by introduce the rare earth oxides to the present glass. This attributed to that the rare earth oxides will enter the glass network as intermediate. The peak around 360 cm^{-1} can

Fig. 5 Variation of Boson peak band position and intensity with composition of the Er-doped glass

be assigned to both TeO_3 tp and/or Er–O bond $[25]$. The formation of Te–O–W bonds is expected, because both Te and W ions have comparable electronegativity values (2.1 and 2, respectively) and can, therefore, substitute for each other in bonding with O atoms. Peak at 930 cm^{-1} is assigned to the WO_4 tetrahedra and/or WO_6 octahedra.

Conclusions

In the present work, tellurite glasses has been prepared according to this formula $(70 - x)TeO₂ - 20WO₃ - 10Li₂O$ $x\text{Ln}_2\text{O}_3$ where $x = 0, 1, 3$ and 5 mol.% and Ln are La, Pr, Nd, Sm, Er and Yb, respectively. The increase in density and molar volume of the present quaternary telluride glasses when the rare earth oxides added is due to the higher molecular weight of the added rare earth oxides than that of $TeO₂$. The density correlated with the calculated cross-link density of the glasses. The Poisson's ratio was also calculated. The calculated number of bonds per unit volume of the glasses was increase and the glass become more rigid. The bond length between the ions of the main structural groups of the glass was calculated and the wavenumber band position of the absorption bands is also calculated. The structure of these glasses is built up from TeO₄ tbp, TeO₃ tp, WO₄ tetrahedral and/or WO₆ octahedra groups. The low frequency Raman absorption band obtained for all the studied samples, which at around 50 cm^{-1} , are identified with Boson peak, a feature characteristic of the vitreous state. This means that the rare earth ions were incorporated in the network of the present glasses and acts as a network intermediate. Also it can be suggested that the present glasses are good host for these rare earth ions and good for optical properties and optical applications.

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